# Optimal Adaptation in Web Processes with Coordination Constraints 

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#### Abstract

We present methods for optimally adapting Web processes to exogenous events while preserving inter-service constraints that necessitate coordination. For example, in a supply chain process, orders placed by a manufacturer may get delayed in arriving. In response to this event, the manufacturer has the choice of either waiting out the delay or changing the supplier. Additionally, there may be compatibility constraints between the different orders, thereby introducing the problem of coordination between them if the manufacturer chooses to change the suppliers. We adopt the paradigm that an abstract Web process flow is pre-specified, and service managers are tasked with interacting with the actual Web services. We focus on the decision making models of the managers who must adapt to external events while satisfying the coordination constraints. We use Markov decision processes as the underlying models for the managers, and show how they can be formulated offline resulting in policies that guide the managers' actions. Our methods range from being centralized and globally optimal in their adaptation but not scalable, to decentralized that is suboptimal but scalable to multiple managers. We also develop a hybrid approach that improves on the performance of the decentralized approach with a minimal loss of scalability.


## Introduction

Recently, there is growing interest in using Web services (WS) as the key building blocks for creating inter- and intra-enterprise business processes. They use the servicesoriented architecture (Casati et al. 2000) as a point of departure, and are called Web processes. Previous work on Web processes has focused largely on configuring or formulating the process flow (Agarwal et al. 2005; Aggarwal et al. 2004; Doshi et al. 2005; Zeng et al. 2003) and developing the associated languages for representing the Web processes (OASIS ). In addition to the problem of composition of Web processes, we must also address the challenges of adaptation, optimality, and recoverability. Together these properties contribute toward more agile and dynamic Web processes. For example, consider a supply chain process where a manufacturer is awaiting merchandise that was ordered previously. If the shipment is delayed, the manufacturer may wait out the delay or it's process may adapt by
possibly canceling the order and choosing a different supplier.
In this paper, we address the problem of optimally adapting Web processes to external events. Adaptation in processes is further complicated in the presence of constraints between services. An example constraint is when the merchandise ordered at different points in the process must be compatible. For example, in a supply chain process that involves ordering computer parts, RAM that is ordered from a memory chip provider service must be compatible with the motherboard that is ordered from another service. Hence, changing the service that provides RAM (perhaps due to a delay in satisfying the order) may need to be coordinated with a change in the service that provides the motherboard.

We present three methods for adapting the process in the face of external events and coordination constraints between participating services. Our methods improve on the previous work by accounting for the uncertainty of events and emphasizing cost-based optimality of decisions. We adopt the paradigm that abstract process flows are pre-defined and proxies, whom we call service managers (SMs), are used to discover and interact with the required Web services (Aggarwal et al. 2004). We focus on the decision models for the managers and for this purpose use stochastic optimization frameworks called Markov decision processes (MDPs) (Puterman 1994). The input to our models is a stochastic state transition machine which represents the possible transitions for each SM, and the costs of the transitions. In our first method, we adopt a global view of the process and formulate a multi-agent MDP model for controlling the SMs. This centralized approach guarantees that the adaptation in response to external events, while respecting the coordination dependencies is globally optimal. However, this approach does not scale well to a large number of SMs. To address the scalability issue, we present a decentralized approach by formulating a MDP model for each individual SM in the process and a mechanism for coordinating between the SMs. However, this approach is no longer globally optimal, and we provide a worst case bound for the loss in optimality. A natural extension is to develop a hybrid approach that follows a middle path between the centralized and decentralized approaches. We briefly outline one such hybrid approach and demonstrate that its performance is better than the decentralized one. We experimentally evaluate our methods using an
example supply chain scenario, and analyze the different decisions that are made by the managers for varying dynamism in the environment.

## Related Work

Much of the earlier work on adaptation concentrated on manually changing traditional processes at both the logic and instance levels. In (Kochut et al. 2003; Reichert \& Dadam 1998) graph based techniques were used to evaluate the feasibility and correctness of changes in the control flow of running instances. Ellis et al. (Ellis, Keddara, \& Rozonberg 1995) used petri-nets for formalizing the instance level changes. In a somewhat similar vein, Aalst and Basten (van der Aalst \& Basten 2002) proposed a petri-net based theory for process inheritance which categorized the types of changes that do not affect other interacting processes. More recently, Muller et al. (Muller, Greiner, \& Rahm 2004) used event-condition-action rules to make changes in running instances. None of these papers have considered the issue of long term optimality of the adaptation, as we do with the help of stochastic optimization frameworks. Our work also addresses the added complexity of inter-service dependencies in a process. Isolated attempts to address inter-task dependencies in processes include (Attie et al. 1993) in which dependencies at the transactional level were enforced using scheduling. In this work, the focus was on generating feasible schedules without emphasis on being optimal. This and other works (Krishnakumar \& Sheth 1995; Rusinkiewicz \& Sheth 1995) used task skeletons to represent the transactional semantics of databases and Web services. Our use of probabilistic finite state machines (Markov chains) is a generalization of the task skeletons as used previously.

## Example: Supply Chain

Processes must continuously adapt to stimuli from a dynamic environment to remain optimal. The adaptation is further complicated when different parts of the process are inter-dependent and must coordinate with each other. In order to motivate this problem, consider Dell's supply chain process, as presented in (Kapuscinski et al. 2004). As pointed out in (Kapuscinski et al. 2004), it is crucial for Dell to manage optimal inventory levels of suppliers' inventory centers called revolvers. Dell incurs significant costs if parts in the revolvers run out and its computer production is delayed. On the other hand, a surplus of parts is detrimental to the suppliers. Clearly, an adaptive supply chain process is needed that accounts for delays and switches suppliers if the risk of production delay outweighs the cost of changing suppliers.
We focus on a small but interesting component of the supply chain to illustrate our methods and evaluate them. We consider the supply chain process of a computer manufacturer which operates on minimal inventory, and therefore incurs significant costs if its order is delayed. The computer manufacturer typically orders in bulk different computer parts from different suppliers. Since the parts must be assembled into a single computer, they must be compatible


Figure 1: An example supply chain process of a computer manufacturer.
with each other. For example, the RAM must inter-operate with the motherboard (see Fig. 1). Therefore, if the delivery of the RAM is delayed and the manufacturer chooses to change the RAM supplier, the supplier of the motherboard must also be changed to preserve the compatibility constraint. ${ }^{1}$
As an example of the type of choice involved in this process, in deciding to change the RAM supplier the manufacturer must take into account the consequences in terms of cost of ordering the motherboard from a new compatible supplier too. Of course, the cost of switching suppliers will vary with the state of the process. For example, if the delivery of the RAM is delayed and the motherboard has arrived, then a decision to change the RAM supplier would entail returning back the motherboard and changing the motherboard supplier. Such a decision might prove more costly than waiting out the delay in receiving the RAM. Additionally, the new supplier may also suffer a delay. The problem is to adapt optimally to the external events like delay while respecting the constraints.

## Web Process Architecture

We adopt METEOR-S (Aggarwal et al. 2004; Verma et al. 2005b) as the services-oriented architecture, within which we implement the Web process. In this section, we briefly outline the relevant components of the architecture, and refer the interested reader to (Aggarwal et al. 2004; Verma et al. 2005b) for further details. METEOR-S creates a virtual layer over a WS-BPEL (OASIS ) Web process engine that allows dynamic configuration and run-time execution of abstract Web processes. This is done with the help of an execution environment and a configuration module. The execution environment consists of SMs that control the interaction with a particular discovered WS(s). An optional process manager (PM) is responsible for global oversight of the process. From the implementation point of view, when the process engine makes a call to a WS - described using WSDL-S (Akkiraju et al. ) - it is routed to the SM. Based on the semantic template associated with the call, the SM utilizes the configuration module to discover services that match the template, and identify the compatible sets.
While the SMs in METEOR-S exhibit the capabilities of

[^0]dynamic discovery and binding of WSs to abstract processes and possess some recovery capabilities from service failures, they are unable to adapt to logical failures in their interactions with WSs. Logical failures include domain specific application level failures such as a delay in delivery of ordered goods in a supply chain process. In this paper, we present approaches that allow the METEOR-S framework to adapt to logical failures.

## Background: Markov Decision Processes

Markov decision processes (MDPs) (Puterman 1994) are well known and intuitive frameworks for modeling sequential decision making under uncertainty. In addition to modeling the uncertainty that pervades real world environments, they also provide a way to capture costs and thereby guarantee cost-based optimality of the decisions. An MDP is formally a tuple:

$$
M D P=\langle S, P A, T, C, O C\rangle
$$

where $S$ is the set of states of the process. $P A: S \rightarrow \mathcal{P}(A)$ is a function that gives the set of actions permissible from a state. Here, $A$ is the set of possible actions and $\mathcal{P}(A)$ is its power set. $T: S \times A \times S \rightarrow[0,1]$ is the Markovian transition function which models the probability of the resulting state on performing a permitted action from some local state $\left(\operatorname{Pr}\left(s^{\prime} \mid s, a\right)\right) . C: S \times A \rightarrow \mathbb{R}$ is the cost function which gives the cost of performing an action in some state of the process. The parameter, $O C$, is the optimality criterion. In this paper, we minimize the expected cost over a finite number of steps, $n \in \mathbb{N}$, also called the horizon. Additionally, each unit of cost incurred one step in the future is equivalent to $\gamma$ units at present. $\gamma \in[0,1]$ is called the discount factor with lower values of $\gamma$ signifying less importance on future costs.

We solve the MDP offline to obtain a policy. The policy is a prescription of the action that is optimal given the state of the process and the number of steps to go. Formally, a policy is, $\pi: S \times \mathbb{N} \rightarrow A$ where $S$ and $A$ are as defined previously, and $\mathbb{N}$ is the set of natural numbers. The advantage of a policy-based approach is that no matter what the state of the process is, the policy will always prescribe the optimal action. In order to compute the policy, we associate each state with a value that represents the long term expected cost of performing the optimal policy from that state. Let $V: S \times \mathbb{N} \rightarrow \mathbb{R}$ be the function that associates this value to each state. Then,

$$
\begin{gather*}
V_{n}(s)=\min _{a \in P A(s)} Q_{n}(s, a) \\
Q_{n}(s, a)=C(s, a)+\gamma \sum_{s^{\prime}} T\left(s^{\prime} \mid s, a\right) V_{n-1}\left(s^{\prime}\right) \tag{1}
\end{gather*}
$$

Note that $\forall_{s \in S}, V_{0}(s)=0$. Here, $n \in \mathbb{N}$ is the finite number of steps to be performed. The optimal action from each state is the one that optimizes the value function:

$$
\begin{equation*}
\pi_{n}(s)=\underset{a \in P A(s)}{\operatorname{argmin}} Q_{n}(s, a) \tag{2}
\end{equation*}
$$

## Centralized Approach: M-MDP

Our first approach adopts a global view of the Web process; we assume that a central process manager (PM) is tasked with the responsibility of controlling the interactions of the SMs with the WSs. The advantage of a centralized approach to control is that we are able to guarantee global optimality of the service managers' decisions while respecting the coordination constraints. We illustrate the approach using Fig. 2


Figure 2: The PM does the global decision making for adaptation using the M-MDP model.

## Model

We model the PM's decision problem as a multi-agent MDP (M-MDP). M-MDPs generalize MDPs to multi-agent settings by considering the joint actions of the multiple agents.

For the sake of simplicity, we consider two SMs, $i$ and $j$. Our model may be extended to more SMs in a straightforward manner. We formalize the PM as a M-MDP:

$$
\mathcal{P M}=\langle S, P A, T, C, O C\rangle
$$

where: - $S$ is the set of global states of the Web process. Often it is possible to define the global state using a factored representation where the factors are the SMs' local states.
Definition 1 (Factored State) The global state space may be represented in its factored form: $S=S_{i} \times S_{j}$. Here, each global state $s \in S$ is, $s=\left\langle s_{i}, s_{j}\right\rangle$, where $s_{i} \in S_{i}$ is the local state (or the partial view) of $S M i$, and $s_{j} \in S_{j}$ is the local state of $S M j$.
Definition 2 (Locally Fully Observable) A process is locally fully observable if each SM fully observes its own state, but not the state of the other manager.

Since the global state is factored with each manager's local state as its components, the PM may combine the local observations so as to completely observe the global state.

- $P A: S \rightarrow \mathcal{P}(A)$ where $A=A_{i} \times A_{j}$ is the set of joint actions of all the SMs and $\mathcal{P}(A)$ is the power set of $A$. The actions include invocations of WS operations. $P A(s)$ is as defined previously in Section. Using Definition 1, we may decompose $P A(s)$ as: $P A(s)=P A_{i}\left(s_{i}\right) \times P A_{j}\left(s_{j}\right)$ where $P A_{i}\left(s_{i}\right)$ and $P A_{j}\left(s_{j}\right)$ are the sets of permitted actions of the SMs $i$ and $j$ from their individual states $s_{i}$ and $s_{j}$, respectively.
- $T: S \times A \times S \rightarrow[0,1]$ is the transition function which captures the global uncertain effect of joint actions of the SMs. Often the actions of each SM affect only its own state and the global state space being factored, we may decompose the global transition function into its components.
Definition 3 (Transition Independence) The global transition function, $T\left(s^{\prime} \mid s, a\right), a \in P A(s)$, may be decomposed:

$$
\begin{align*}
T\left(s^{\prime} \mid s, a\right) & =\operatorname{Pr}\left(\left\langle s_{i}^{\prime}, s_{j}^{\prime}\right\rangle \mid\left\langle s_{i}, s_{j}\right\rangle,\left\langle a_{i}, a_{j}\right\rangle\right) \\
& =\operatorname{Pr}\left(s_{i}^{\prime} \mid s_{j}^{\prime},\left\langle s_{i}, s_{j}\right\rangle,\left\langle a_{i}, a_{j}\right\rangle\right) \cdot \operatorname{Pr}\left(s_{j}^{\prime} \mid\left\langle s_{i}, s_{j}\right\rangle,\left\langle a_{i}, a\right.\right. \\
& =T_{i}\left(s_{i}^{\prime} \mid s_{i}, a_{i}\right) \cdot T_{j}\left(s_{j}^{\prime} \mid s_{j}, a_{j}\right) \tag{3}
\end{align*}
$$

where $T_{i}, T_{j}$ are the individual SM's transition functions, $a_{i} \in P A_{i}\left(s_{i}\right), a_{j} \in P A_{j}\left(s_{j}\right)$, and $s_{i}^{\prime}$ and $s_{j}^{\prime}$ are the next states of $i$ and $j$, respectively. In other words, we assume that, $\operatorname{Pr}\left(s_{i}^{\prime} \mid\left\langle s_{i}, s_{j}\right\rangle,\left\langle a_{i}, a_{j}\right\rangle, s_{j}^{\prime}\right)=\operatorname{Pr}\left(s_{i}^{\prime} \mid s_{i}, a_{j}\right)$, and $\operatorname{Pr}\left(s_{j}^{\prime} \mid\left\langle s_{i}, s_{j}\right\rangle,\left\langle a_{i}, a_{j}\right\rangle\right)=\operatorname{Pr}\left(s_{j}^{\prime} \mid s_{j}, a_{j}\right)$, because each SM's next state is influenced only by its own action and its current state.

- $C: S \times A \rightarrow \mathbb{R}$ is the cost function. This function captures the global cost of invoking the WSs by the SMs based on the global state of the process. These costs may be obtained from the service level agreements (Ludwig et al. 2003) between the enterprise whose process is being modeled and the service providers. In our example, the cost function would capture not only the costs of invoking the WSs, but also the cost of waiting for the delayed order and changing the supplier. As we mentioned before, the possible change of supplier by one SM must be coordinated with the other SM, to preserve the product compatibility constraints. Coordination is enforced by incurring a very high global cost if only one SM changes its supplier. This high cost signifies the penalty of violating the product compatibility constraint.
- $O C$ is the optimality criterion as defined in Section .

Let us utilize the M-MDP formalism introduced previously, to model the supply chain example.
Example 1 An example global state of the process is $\langle\underbrace{\mathbf{O} \overline{\mathbf{D}} \overline{\mathrm{CS}} \overline{\mathbf{R}}}_{i}, \underbrace{\mathrm{OD} \overline{\mathrm{CS}} \overline{\mathbf{R}}}_{j}\rangle$. This global state denotes that $i$ has placed an order $(\mathbf{O})$ that has not yet been delayed $(\overline{\mathbf{D}})$, the supplier has not been changed (CS), and i has not yet received the order $(\overline{\mathbf{R}})$. SM $j$ has placed an order that has been delayed but not changed its supplier. Possible actions for each $S M$ are the same: $A_{i}=A_{j}=\{\operatorname{Order}(\mathrm{O})$, Wait (W), ChangeSupplier (CS) \}. The action Order denotes the invocation of the relevant $W S(s)$ of the chosen supplier to place an order, Wait is similar to a no operation (NOP), and ChangeSupplier signifies the invocation of the relevant WSs to cancel the order or return it (if received), and select a new compatible supplier. A partial cost function is shown in Fig. 3(b), and the transition function for an individual SM is discussed next.

## Exogenous Events

In our example supply chain scenario, the manufacturer must act in response to several events such as a notification of delay from the supplier and a notification of receipt of the order. In order to ensure that the SM responds to these
events optimally, they must be a part of our model. Since the events are external to the Web process, we label them as exogenous.
In order to model the exogenous events, we perform two steps: (1) We specify expanded transition functions for the SMs $i$ and $j$. In other words, $T_{i}^{E}: S_{i} \times A_{i} \times E_{i} \times S_{i} \rightarrow[0,1]$, where $E_{i}$ is the set of mutually exclusive events, and rest of the symbols were defined previously. For our example, $E_{i}=$ $\{$ Delayed, Received, None\}. The expanded transition funcfidn models the uncertain effect of not only the SM's actions but also the exogenous events on the state space. We show the expanded transition function for the SM $i$ in Fig. 3(a). (2) We define $a$ 'priori a probability distribution over the occurrence of the exogenous events conditioned on the state of the SM. For example, let $\operatorname{Pr}($ Delayed $\mid O \bar{D} \overline{C S} \bar{R})=0.45$ be the probability that SM $i$ 's order for RAM is delayed.

We obtain the transition function, $T_{i}$, that is a part of the model defined in Section (see Eq. 3), by marginalizing or absorbing the events. Formally,

$$
T_{i}\left(s_{i}^{\prime} \mid s_{i}, a_{i}\right)=\sum_{e \in E_{i}} T_{i}^{E}\left(s_{i}^{\prime} \mid s_{i}, a_{i}, e\right) \operatorname{Pr}\left(e \mid s_{i}\right)
$$

Here, $T_{i}^{E}$ is obtained from step (1) and $\operatorname{Pr}\left(e \mid s_{i}\right)$ is specified as part of the step (2) above. The marginalized transition function for the SM $i$ is shown in Fig. 4.


Figure 4: A (probabilistic) state transition diagram illustrating the transition function, $T_{i}$, for the SM $i$. Some of the transitions due to the actions are now non-deterministic. The numbers denote the probabilities with which the associated transitions occur.

## Global Policy Computation

Solution of the process manager's model described in Section results in a global policy, $\pi^{*}: S \times \mathbb{N} \rightarrow A$. The global policy prescribes the optimal action that must be performed by each SM given the global state of the Web process and the number of steps to go. Computation of the global policy is analogous to the Eqs. 1 and 2, with $s$ being the global state of the Web process, $a$ the joint action of the SMs, and $T\left(s^{\prime} \mid s, a\right)$ may be decomposed using Eq. 3. During process execution, each SM sends its local state to the PM, who uses the joint state to index into the global policy. The prescribed actions are then distributed to the corresponding SMs for execution.

（a）

| State | $\langle W, W\rangle$ | $\langle W, C S\rangle$ | $\langle C S, W\rangle$ | $\langle C S, C S\rangle$ |
| :---: | :---: | :---: | :---: | :---: |
| $\langle\mathrm{OD} \overline{\mathrm{CS}} \overline{\mathrm{R}}, \mathrm{OD} \overline{\mathrm{CS}} \overline{\mathrm{R}}\rangle$ | 0 | 550 | 550 | 350 |
| $\langle\mathrm{OD} \overline{\mathrm{CS}} \overline{\mathrm{R}}, \mathrm{ODCS} \overline{\mathrm{R}}\rangle$ | 200 | 450 | 750 | 250 |
| $\langle\mathrm{OD} \overline{\mathrm{CS}} \overline{\mathrm{R}}, \mathrm{O} \overline{\mathrm{D}} \overline{\mathrm{CSR}}\rangle$ | 0 | 550 | 550 | 350 |
|  | 0 | 460 | 550 | 260 |
| $\langle\mathrm{ODCS} \overline{\mathrm{R}}, \mathrm{O} \overline{\mathrm{D}} \overline{\mathrm{CS}} \overline{\mathrm{R}}\rangle$ | 200 | 750 | 450 | 250 |
| $\langle\mathrm{ODCS} \overline{\mathrm{R}}, \mathrm{ODCS} \overline{\mathrm{R}}\rangle$ | 400 | 650 | 650 | 150 |
| $\langle\mathrm{ODCS} \overline{\mathrm{R}}, \mathrm{O} \overline{\mathrm{D}} \overline{\mathrm{CSR}}$ 〉 | 200 | 750 | 450 | 250 |
|  | 200 | 710 | 450 | 160 |
|  | 0 | 550 | 550 | 350 |
| $\langle\mathrm{OD} \overline{\mathrm{CSR}}, \mathrm{ODCS} \overline{\mathrm{R}}\rangle$ | 200 | 450 | 750 | 250 |
| 〈OD̄DSR，Ō̄̄̄SR $\rangle$ | －50 | 550 | 550 | 350 |
| 〈OD̄CSR，ODC̄SR ${ }^{\text {O }}$ | －50 | 460 | 550 | 260 |
| $\langle\mathrm{ODCSR}, \mathrm{O} \overline{\mathrm{D}} \overline{\mathrm{CS}} \overline{\mathrm{R}}\rangle$ | 0 | 550 | 460 | 260 |
| 〈ODCSR，ODCSS̄ ） | 200 | 450 | 460 | 160 |
|  | －50 | 550 | 460 | 260 |
| 〈ODCSR，ODC̄SR〉 | －50 | 460 | 460 | 170 |

（b）
Figure 3：（a）A（probabilistic）state transition diagram illustrating the expanded transition function，$T_{i}^{E}$ ，for the $\mathrm{SM} i$ ．Transitions due to actions are depicted using solid lines，and these are deterministic．Exogenous events are shown dashed．For clarity，the occurrence of no event is not shown．The numbers denote example probabilities of occurrence of the events conditioned on the states．（b）The partial cost function for the PM．We show the costs for the more interesting actions of waiting and changing the supplier，for a subset of the states．The cost function penalizes those action combinations where only one SM changes the supplier thus violating the compatibility constraint．

While the centralized approach requires the specification of a global model of the process，the advantage is that we can guarantee the optimality of the global policy．In other words， no other policy for controlling the SMs exists that will incur an expected cost less than that of the global policy．Conse－ quently，the global policy resolves the coordination problem between the SMs in an optimal manner．Theorem 1 formally states this result．Due to the lack of space，the proof of this theorem is given in（Verma et al．2005a）．

Theorem 1 （Global Optimality）The global policy of the $\mathrm{PM}, \pi^{*}$ ，is optimal for the finite horizon discounted opti－ mality criterion．


Figure 5：Example coordination graphs．（a）The worst case coor－ dination graph where all the SMs must coordinate with each other． （b）More realistic case，where only subsets of SMs must coordi－ nate．

Let us consider a Web process where there are，$N>2$ ， SMs．In the worst case，all the SMs may have to coor－ dinate with each other due to，say，the product compat－ ibility constraints（Fig．5（a））．For this case，Eq． 1 be－ comes，$V_{n}(s)=\min _{a \in P A(s)} Q_{n}(s, a)$ ，where $a \in A$ ，and $A=A_{i} \times A_{j} \times A_{k} \times \ldots \times A_{n}$ ．Here，$A_{i}, A_{j}, A_{k}$, $\ldots, A_{n}$ are the action sets of the SMs $i, j, k, \ldots, n$ ，
respectively．More realistically，only subsets of the SMs may have to coordinate with each other，as shown in Fig．5（b）．In this case，$V_{n}(s)=\min Q_{n}^{1}\left(s,\left\langle a_{i}, a_{j}, a_{k}, a_{l}\right\rangle\right)$ $+Q_{n}^{2}\left(s,\left\langle a_{m}, a_{n}\right\rangle\right)=\min _{\left\langle a_{i}, a_{j}, a_{k}, a_{l}\right\rangle}{ }^{a} Q_{n}^{1}\left(s,\left\langle a_{i}, a_{j}, a_{k}, a_{l}\right\rangle\right)+$ $\min _{\left\langle a_{m}, a_{n}\right\rangle} Q_{n}^{2}\left(s,\left\langle a_{m}, a_{n}\right\rangle\right)$ ．

## Decentralized Approach：MDP－CoM

While adopting a global view of the process guarantees a globally optimal adaptation and coordination between the SMs，the approach does not scale well to many services in the process．This is because the decision making by the process manager must take into account the possible actions of all the coordinating SMs．Of course，this is exponential in the number of SMs．As we mentioned previously，in the worst case this might involve all the SMs．In this section，we present a decentralized approach that scales reasonably well to multiple managers，but in doing so we lose the global op－ timality of the adaptation．This approach is made possible due to the properties of transition independence and local full observability exhibited by the process．
Our approach is based on formulating a MDP model for each individual SM，thereby allowing each SM to make its own decision．We assume that all the SMs act at the same time step，and actions of the other SMs are not observable． Since coordination between the SMs that reflects the inter－ service dependency is of essence，we define a mechanism for ensuring the coordination．Each SM，in addition to fully ob－ serving its local state，also observes the coordination mech－ anism（CoM）perfectly（Fig．6）．


Figure 6: Each SM locally decides its action in response to the events. The SMs coordinate using a CoM that each observes perfectly.

## Model

We model each SM's decision making process as a MDP. The MDP model for a SM, say $i$, is:

$$
\mathcal{S} \mathcal{M}_{i}=\left\langle S_{i}, P A_{i}, T_{i}, C_{i}, O C_{i}\right\rangle
$$

where: $\bullet S_{i}$ is the set of local states of the $\mathrm{SM} i . \bullet P A_{i}$ : $S_{i} \rightarrow \mathcal{P}\left(A_{i}\right)$, gives the permissible actions of the SM for each of its local states. An action may be the invocation and use of a WS. $\bullet T_{i}: S_{i} \times A_{i} \times S_{i} \rightarrow[0,1]$, is the local transition function. $\bullet C_{i}: S_{i} \times A_{i} \rightarrow \mathbb{R}$, is the $\mathrm{SM} i$ 's cost function. This function gives the cost of performing an action from some state of the SM. $\bullet O C_{i}$ is the SM $i$ 's optimality criterion. In this paper, we assume that each of the SMs optimizes w.r.t. a discounted finite horizon, though in general they could have different optimality criteria. For our supply chain example, the MDP for the SM $i$ is given below.
Example 2 An example local state of the SM is ODCS $\overline{\mathbf{R}}$ which denotes that $i$ has placed an order that has been delayed, but it has not changed its supplier. Possible actions for the $S M$ i are: $A_{i}=\{\operatorname{Order}(\mathrm{O})$, Wait (W), ChangeSupplier (CS) \}. The semantics of these actions are as defined previously in Example 1. The transition function was shown previously in Fig. 4, and the partial cost function is shown in Table. 1.

| State | $W$ | $C S$ |
| :---: | :---: | :---: |
| O$\overline{\mathbf{D C S}} \overline{\mathbf{R}}$ | 0 | 200 |
| OD $\overline{\mathrm{CSR}} \overline{\mathbf{R}}$ | 250 | 150 |
| O$\overline{\mathbf{D C S R}}$ | -50 | 250 |
| ODCSR | -50 | 175 |

Table 1: A partial cost function for the $\mathrm{SM} i$.
The exogenous events that include a delay in receiving the order and a notification of receipt of the order, are handled in a similar manner as described in Section. In other words, we expand the SM's local transition function to include the events. As we mentioned before, the events may alter the local state of the SM.

## Coordination Mechanism

In our decentralized approach, each SM arrives at its own decision on how to best respond to the exogenous events. Since the decision making is local, we must define a mechanism to ensure coordination between the SMs in order to preserve the coordination constraint. As an example, if the SM that is ordering RAM decides to change its supplier, then the SM ordering the motherboard must follow suit, no matter whether it's an optimal decision for the other SM. This is precisely the source of the loss in optimality for our decentralized approach.

While mechanisms for coordinating between the SMs manifest in various forms, one such mechanism is a finite state machine (FSM), whose state is perfectly observable to all the SMs. We may define the FSM to have two general states: an uncoordinated $(\mathrm{U})$ state and a coordinated (C) state. The state of the FSM signifies whether the SMs must coordinate. Formally, the FSM is a tuple $\langle Y, A, \tau\rangle$, where $Y$ is the set of states of the FSM, $Y=\{\mathrm{U}, \mathrm{C}\} . A$ is the set of joint actions of the SMs defined previously. Here, $\tau: Y \times A \times Y \rightarrow[0,1]$ is the transition function of the FSM. Initially the actions of the SMs are uncoordinated each SM is free to follow the optimal action conditioned on its local state. We assume that if a SM decides to change the supplier, it must signal its intent first. ${ }^{2}$ When any SM signals its intent to change the supplier, the FSM transitions to the coordinated state. When the FSM is in this state, all SMs are required to change their suppliers immediately. Their actions will also reset the FSM back to the uncoordinated state. We show the FSM in Fig. 7.


Figure 7: FSM for coordinating between the SMs. Transitions (solid arrows) are caused by the joint actions of the SMs. '*' indicates any action of a SM, while '?' indicates the remaining actions. The dashed arrow gives the action rule for each SM when the FSM is in that state.

## Expanded Model

To ensure coordination, the CoM must be included in the SM's decision making process. We do this by combining the MDP model that was defined previously in Section, with the CoM and call the new model, MDP-CoM. Within the MDPCoM , the state space is expanded to include the states of the CoM as well: $\hat{S}_{i}=S_{i} \times Y$. The action choices available to the SM are, $A_{i}^{\prime}=A_{i} \cup\{$ Intent $\}$. To ensure that the SM changes the supplier iff the FSM is in the coordinated (C) state, we define the function, $\hat{P A_{i}}(\langle *, C\rangle)=C S$, and remove the choice of changing the supplier when the FSM is in the uncoordinated state, $\hat{P A_{i}}\left(\left\langle s_{i}, U\right\rangle\right)=P A_{i}\left(s_{i}\right) / C S$. Here, ${ }^{\prime}{ }^{\prime}$ 's stands for any local state of the SM $i$.

[^1]The transition function is the joint defined as: $\hat{T}_{i}: \hat{S}_{i} \times$ $A_{i} \times \hat{S}_{i} \rightarrow[0,1]$. Here,

$$
\begin{align*}
\hat{T}_{i}\left(\left\langle s_{i}^{\prime}, y^{\prime}\right\rangle \mid a_{i},\left\langle s_{i}, y\right\rangle\right) & =\operatorname{Pr}\left(s_{i}^{\prime} \mid y^{\prime}, a_{i},\left\langle s_{i}, y\right\rangle\right) \operatorname{Pr}\left(y^{\prime} \mid a_{i},\left\langle s_{i}, y\right\rangle\right) \\
& =T_{i}\left(s_{i}^{\prime} \mid a_{i}, s_{i}\right) \operatorname{Pr}\left(y^{\prime} \mid a_{i}, y\right) \tag{4}
\end{align*}
$$

Since the next state of the CoM depends on actions of both the SMs, and the SM $i$ does not observe the other SM's actions, we must average over the other's actions: $\operatorname{Pr}\left(y^{\prime} \mid a_{i}, y\right)=\sum_{a_{j}} \operatorname{Pr}\left(y^{\prime} \mid a_{i}, a_{j}, y\right) \operatorname{Pr}\left(a_{j} \mid a_{i}, y\right)=$ $\sum_{a_{j}} \tau\left(y^{\prime} \mid a_{i}, a_{j}, y\right) \operatorname{Pr}\left(a_{j} \mid y\right)$

When the state of the CoM is $C$, the $\mathrm{SM} i$ knows that everyone must change their respective suppliers, and therefore $\operatorname{Pr}\left(a_{j}=C S \mid y=C\right)=1$. On the other hand, when the state is $U$, we assume that $i$ has no knowledge of the other's decision making model and therefore assumes that each of SM $j$ 's actions are equally probable. The cost function, $\hat{C}_{i}: \hat{S}_{i} \times A_{i} \rightarrow \mathbb{R}$, gives the cost of acting from the combined local state and the state of the CoM. However, for our purposes, the state of the CoM does not matter in deciding the cost.

## Local Policy Computation

We associate with each local state of the SM and the state of the CoM, a value function that gives the expected cost of following an optimal policy from that state. Equation 1 forms the basis for computing the value function, while Eq. 2 computes the optimal policy for the MDP-CoM model, $\pi^{i}: \hat{S}_{i} \times \mathbb{N} \rightarrow A_{i}$. Note that in these equations, we use the expanded model described in Section .
While the decentralized approach scales well for multiple SMs since each SM does its own decision making, the trade off is our inability to guarantee global optimality. This is because, a SM's decision does not take into account the state, actions, and costs of the other SM. For the supply chain example, SM $i$ 's intent to change the supplier would necessitate a change of supplier for $j$ as well irrespective of the fact that the action may not be optimal for $j$. We calculate a bound for the error that would be introduced in this case. Let $\epsilon_{n}$ be the error bound, then, $\epsilon_{n}=\left\|V_{n}^{i}-\hat{V}_{n}^{i}\right\|_{\infty}$, where $\|\cdot\|_{\infty}$ is the max norm, $V_{n}^{i}$ is the value function for the MDP model, and $\hat{V}_{n}^{i}$ is the value function for the MDP-CoM model. The difference can be bounded as, $\epsilon_{n}=\frac{\left(C_{i, \text { max }}-C_{i, \text { min }}\right)\left(1-\gamma^{n}\right)}{1-\gamma}$, where $C_{i, \min }$ and $C_{i, \max }$ are the least and maximum costs, respectively. Note that a SM may suffers the maximum loss in optimality when trying to respect the coordination constraint. Due to lack of space, we give the proof of this error bound in (Verma et al. 2005a). In order to calculate the loss with respect to the globally optimal policy, for the simple case where $C(s, a)=C_{i}\left(s_{i}, a_{i}\right)+C_{j}\left(s_{j}, a_{j}\right)$, the error bound $\epsilon_{n}$ also represents the worst case loss from global optimality. We note that this error bound does not scale well to many SMs. In general, for $N \mathrm{SMs}$, the worst case error bound is $(N-1) \epsilon_{n}$.

## Hybrid Approach: H-MDP-CoM

Our hybrid approach uses the MDP-CoM model as a point of departure, but improves on its error bounds by allowing the PM to step in during runtime and exercise some control over the SMs' actions when coordination is required. For example, when any SM intends to change the supplier, the PM decides whether or not to allow the action based on its global optimality for all the SMs.

## Model

In order to enable the PM's decision, each SM sends to the PM, its action-value function for the optimal action as well as the other action alternatives. For the supply chain example, when an SM, say $i$, declares its intent to change its supplier, it must send to the PM, $Q_{n}^{i}\left(\left\langle s_{i}, y\right\rangle, C S\right)$ and $Q_{n}^{i}\left(\left\langle s_{i}, y\right\rangle, W\right)$, where $s_{i}$ and $y$ are the current states of the $\mathrm{SM} i$ and the CoM, respectively, and $Q_{n}^{i}$ is the action-value function. We denote this action as sendQ, and is added to the previously defined space of actions of each SM. ${ }^{3}$ This sequence of behavior is enforced by the CoM, as shown in Fig. 8. Since the decision making is shared with the PM, the transitions of the CoM are also dependent on the PM's actions. Specifically, at state $M$ of the CoM, if the PM decides that all the SMs should change their suppliers, the mechanism will transition to state $C_{2}$. On the other hand, the PM may ask the SM that declared its intent to wait out the delay represented by state $C_{1}$ of the CoM.


Figure 8: The CoM for our hybrid approach.

## Hybrid Policy Computation

Computing the local policy for each SM is analogous to the corresponding computation in the MDP-CoM model. The primary difference is in the generation of the local transition function, $\hat{T}_{i}$, shown in Eq. 4 that encompasses the transitions of the CoM. In addition to averaging over the actions of the other SM, $i$ must also average over the PM's possible actions. However, the averaging is considerably simplified when we observe that the PM's action matters only when the CoM is in the $M$ state. The net result is a local policy which defers the deliberation over the coordinating action to the PM.
The issue remaining to be resolved is the runtime decision process of the PM, when any of the SM declares its intent to do a coordinating action. For our example, if $i$

[^2]does so, then the PM opts for a CS, if $Q_{n}^{i}\left(\left\langle s_{i}, M\right\rangle, C S\right)+$ $Q_{n}^{j}\left(\left\langle s_{j}, M\right\rangle, C S\right)>Q_{n}^{i}\left(\left\langle s_{i}, M\right\rangle, W\right)+Q_{n}^{j}\left(\left\langle s_{j}, M\right\rangle, a_{j}^{*}\right)$, where $a_{j}^{*}$ is the SM $j$ 's optimal action at $\left\langle s_{j}, M\right\rangle$. For this case, the CoM transitions from state $M$ to $C_{2}$. Otherwise, the PM instructs $i$ to simply wait out the delay ( $\mathbf{W}$ ), because this is less expensive globally (in the long term) than all the SMs changing their suppliers. The CoM then transitions from state $M$ to $C_{1}$.

## Empirical Evaluation

We empirically evaluate our methods using the supply chain introduced in Section. We implemented all of the models within the METEOR-S framework described previously in Section. A method to represent inter-service coordination constraints such as ours, in WS-BPEL is given in (Verma et al. 2004). As part of our evaluation, we first show that the value function of the M-MDP model (Section ) is monotonic and converges over an increasing number of horizons. Naturally, this implies that the policy, $\pi^{*}$, of the PM also converges. The convergence is reflected by the gradual flattening of the curves in the plot shown in Fig. 9. Though we show the values for a subset of the states, this behavior is true for all the states. Additionally, similar convergences are demonstrated by the value functions of the MDP-CoM and the hybrid models as well.


Figure 9: Convergence of the value function of the M-MDP model.

The second part of our evaluation focuses on studying the adaptive behaviors of our models in environments of varying volatility. These environments are characterized by increasing probabilities of occurrence of an external event such as a delay, and increasing penalties to the manufacturer for waiting out the delay. Our benchmark (null hypothesis) is a random policy in which each SM randomly selects between its actions, and if it elects to change the supplier, all SMs follow suit to ensure product compatibility. Our methodology consisted of plotting the average costs incurred by executing the policies generated by solving each of the models for different probabilities of receiving a delay event and across varying costs of waiting out a delay. The costs were averaged over a trial of 1000 runs and each trial was performed 10 times.
We show the plots for the different costs of waiting in case of a delay in Fig. 10. We computed all of our policies for 25 steps to go. When the cost of waiting for each SM in response to a delay is low, as in

Fig, 10(a), all of our models choose to wait out the delay. For example, $\pi_{n}^{*}(\langle\mathbf{O D C S} \overline{\mathbf{R}}, \mathbf{O D} \overline{\mathbf{C S}} \overline{\mathbf{R}}\rangle)=\langle W, W\rangle$, and $\pi_{n}^{i}(\langle\mathbf{O D C S} \overline{\mathbf{R}}, U\rangle)=\pi_{n}^{j}(\langle\mathbf{O D C S} \overline{\mathbf{R}}, U\rangle)=W$. Of course, the random policy incurs a larger average cost since it randomizes between waiting and changing the suppliers. When the penalty for waiting out the delay is 300 which is greater than the cost of changing the supplier (Fig. 10(b)), the behaviors of the models start to differ. Specifically, due to its global view of the process, the M-MDP model does the best - always incurring the lowest average cost. For low probabilities of the order being delayed, the M-MDP policy chooses to change the supplier in response to a delay, since it's less expensive in the long term. However, as the chance of the order being delayed increases, the M-MDP policy realizes that even if the SMs change the suppliers, the probability of the new suppliers getting delayed is also high. ${ }^{4}$ Therefore it is optimal for the SMs to wait out the delay for high delay probabilities. The performance of the MDPCoM reflects its sub-optimal decision-making. In particular, it performs slightly worse than the random policy for low delay probabilities. This is due to the SM $i$ always choosing to change the supplier in response to the delay and the CoM ensuring that the SM $j$ changes its supplier too. For states where $j$ has already received the order, this action is costly. Note that the random policy chooses to change the supplier only some fraction of the times. For larger delay probabilities, the MDP-CoM policy adapts to waiting in case of a delay, and hence starts performing better than the random policy. The performance of the hybrid approach is in between that of the M-MDP and the MDP-CoM models, as we may expect. By selecting to change the suppliers only when it is optimal globally, the hybrid approach avoids some of the pitfalls of the decentralized approach. For an even larger cost of waiting out the delay, as in Fig. 10(c), the MDP-CoM policy chooses to change the supplier up to a delay probability of 0.5 , after which the policy chooses to wait when delayed. As we mentioned previously, a large delay probability means that the expected cost of changing the supplier is large since the new supplier may also be delayed with a high probability. Hence, the policy chooses to wait out the delay, rather than change the supplier and risk being delayed again.
In summary, the centralized M-MDP model for the process manager performs the best since it has complete knowledge of the states, actions, and costs of all the SMs. This supports our Thm. 1. The MDP-CoM does slightly worse than the random policy for low delay probabilities, but improves its performance thereafter. The maximum difference between its average behavior and that of the globally optimal M-MDP model is 234.8 which is much less than the difference calculated using our theoretical error bound, $\epsilon_{n}$ $=2784.6$. This is because of the worst case nature of our error bound analysis. The hybrid approach does better than the MDP-CoM and the random policy, but worse than the

[^3]

Figure 10: Line plots showing the average costs incurred for increasing probabilities of the order being delayed and increasing costs of waiting for the order in response to the delay. The vertical lines in each plot show the standard deviations.

M-MDP. We also point out that the maximum percentage improvement of our M-MDP model in comparison to the random policy was $31.3 \%$.


Figure 11: Run times for solving the models and generating the policies. The times were computed on a PIV 3GHz, 1 GB RAM, and Win XP.

Finally, we address the scalability of our models to larger number of SMs. We show the time taken to solve the different models in a histogram plot, Fig. 11, for increasing number of SMs. As we mentioned previously, the complexity of the M-MDP model is exponential with respect to the number of SMs. This is demonstrated by the exponential increases in time taken for computing the M-MDP policy as the number of SMs increases from 2 to 5 . In comparison, the time taken to solve the MDP-CoM and the hybrid models increases linearly. For the latter models, we report the total time taken to compute the policies for all the SMs. More realistically, for the decentralized and the hybrid approaches, the models for the SMs may be solved in parallel, and hence there is no increase in the net run times. Note that the CoM also scales well to multiple SMs. Specifically, no increase in the number of states of the FSM is required for more SMs, though the communication overhead increases.

## Conclusion

As businesses face more dynamism and processes become more complex, methods that address adaptation while preserving the complex inter-service constraints have gained importance. Past approaches to this problem have tackled either adaptation to exogenous events or enforcing interservice constraints, but not both. Additionally, these approaches have ignored optimality considerations. In this pa-
per, we presented a suite of stochastic optimization based methods for adapting a process to exogenous events while preserving simple coordination constraints. These methods were presented within the METEOR-S framework of Web processes. In our first method, we adopted a global view of the process and formulated the M-MDP model that guaranteed global optimality in adapting while preserving the constraints. To address the scalability issue, we presented a decentralized approach, MDP-CoM, and bounded its loss of optimality. Our third approach synergistically combines the two approaches so as to promote scalability as well as curtail the worst case loss of optimality. We experimentally evaluated their performances in environments of varying dynamism.

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[^0]:    ${ }^{1}$ It's possible that the RAM from a new supplier might be compatible with the existing motherboard, or the same RAM supplier can provide another compatible RAM in time. However, to focus on the coordination constraint, we do not consider these alternatives, but they can easily be accommodated.

[^1]:    ${ }^{2}$ This behavior would require an additional action denoting the intent, which we address later.

[^2]:    ${ }^{3}$ We assume that the SMs are able to communicate with the PM without any loss of information, though there may be a communication cost.

[^3]:    ${ }^{4}$ We assume for simplicity that the new supplier also has the same probability for being delayed. In general, different suppliers would have different probabilities of being delayed in meeting the order.

